

## SOLUTION EXPERIMENT I

### PART A

#### 1. [Total 0.5 pts]

The experimental method chosen for the calibration of the arbitrary scale is a simple pendulum method [0.3 pts]

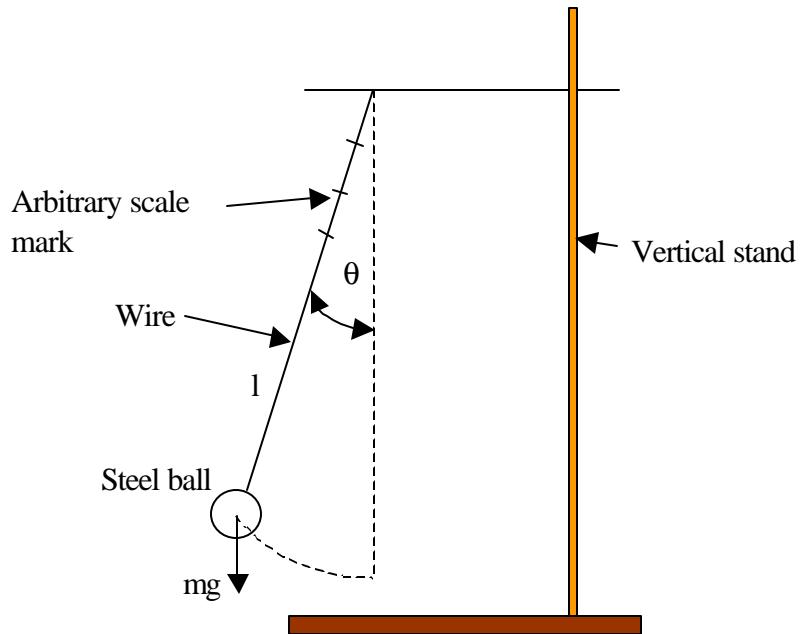


Figure 1. Sketch of the experimental set up [0.2 pts]

#### 2. [Total 1.5 pts]

The expression relating the measurable quantities: [0.5 pts]

$$T_{osc} = 2\pi \sqrt{\frac{l}{g}}; T_{osc}^2 = 4\pi^2 \frac{l}{g}$$

Approximations :

$$\sin q \approx q \quad [0.5 \text{ pts}]$$

mathematical pendulum (mass of the wire << mass of the steel ball,  
the radius of the steel ball << length of the wire [0.5 pts])

flexibility of the wire, air friction, etc [0.1 pts, only when one of the two  
major points above is not given]

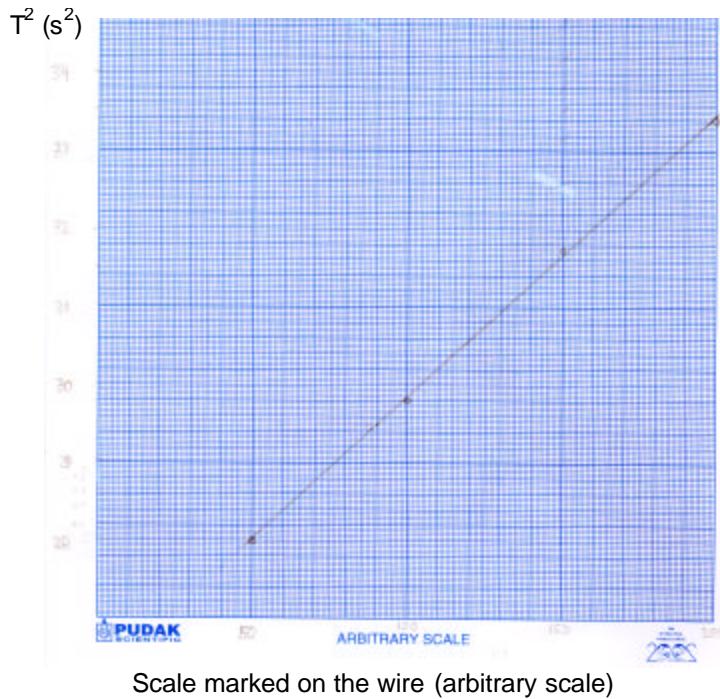
3. [Total 1.0 pts] Data sample from simple pendulum experiment  
 # of cycle  $\geq 20$  [0.2 pts.] , difference in T  $\geq 0.01$  s [0.4 pts], # of data  $\geq 4$  [0.4 pts]

| No. | t(s) for 50 cycles | Period, T (s) | Scale marked on the wire (arbitrary scale) |
|-----|--------------------|---------------|--|
| 1   | 91.47              | 1.83          | 200  |
| 2   | 89.09              | 1.78          | 150  |
| 3   | 86.45              | 1.73          | 100  |
| 4   | 83.8               | 1.68          | 50   |

4. [Total 0.5 pts]

| No. | Period, T (s) | Scale marked on the wire (arbitrary scale) | $T^2(s^2)$ |
|-----|---------------|--|------------|
| 1   | 1.83          | 200  | 3.35       |
| 2   | 1.78          | 150  | 3.17       |
| 3   | 1.73          | 100  | 2.99       |
| 4   | 1.68          | 50   | 2.81       |

The plot of  $T^2$  vs scale marked on the wire:



Scale marked on the wire (arbitrary scale)

5. Determination of the smallest unit of the arbitrary scale in term of mm [Total 1.5 pts]

$$T_{osc_1}^2 = \frac{4\mathbf{P}^2}{g} L_1, \quad T_{osc_2}^2 = \frac{4\mathbf{P}^2}{g} L_2$$

$$(T_{osc_1}^2 - T_{osc_2}^2) = \frac{4\mathbf{P}^2}{g} L_1 - L_2 = \frac{4\mathbf{P}^2}{g} \Delta L$$

$$\Delta L = \frac{g}{4p^2} (T_{osc_1}^2 - T_{osc_2}^2) \text{ or other equivalent expression} \quad [0.5 \text{ pts}]$$

| No. |  | Calculated $\Delta L$ (m) | $\Delta L$ in arbitrary scale | Values of smallest unit of arbitrary scale (mm) |
|-----|--|---------------------------|-------------------------------|---|
| 1.  | $T_1^2 - T_2^2 = 0.171893 \text{ s}^2$ | 0.042626                  | 50                            | 0.85  |
| 2.  | $T_1^2 - T_3^2 = 0.357263 \text{ s}^2$ | 0.088595                  | 100                           | 0.89  |
| 3.  | $T_1^2 - T_4^2 = 0.537728 \text{ s}^2$ | 0.133347                  | 150                           | 0.89  |
| 4.  | $T_2^2 - T_3^2 = 0.18537 \text{ s}^2$  | 0.045968                  | 50                            | 0.92  |
| 5.  | $T_2^2 - T_4^2 = 0.365835 \text{ s}^2$ | 0.09072                   | 100                           | 0.91  |
| 6.  | $T_3^2 - T_4^2 = 0.180465 \text{ s}^2$ | 0.044752                  | 50                            | 0.90  |

The average value of smallest unit of arbitrary scale,  $\bar{l} = 0.89 \text{ mm}$  [0.5 pts]

The estimated error induced by the measurement: [0.5 pts]

| No. | Values of smallest unit of arbitrary scale (mm) | $(l - \bar{l})$ | $(l - \bar{l})^2$ |
|-----|---|-----------------|-------------------|
| 1.  | 0.85  | -0.04           | 0.0016            |
| 2.  | 0.89  | 0               | 0                 |
| 3.  | 0.89  | 0               | 0                 |
| 4.  | 0.92  | 0.03            | 0.0009            |
| 5.  | 0.91  | 0.02            | 0.0004            |
| 6.  | 0.90  | 0.01            | 0.0001            |

And the standard deviation is:

$$\Delta l = \sqrt{\frac{\sum_{i=1}^6 (l_i - \bar{l})^2}{N-1}} = \sqrt{\frac{0.003}{5}} = 0.02 \text{ mm}$$

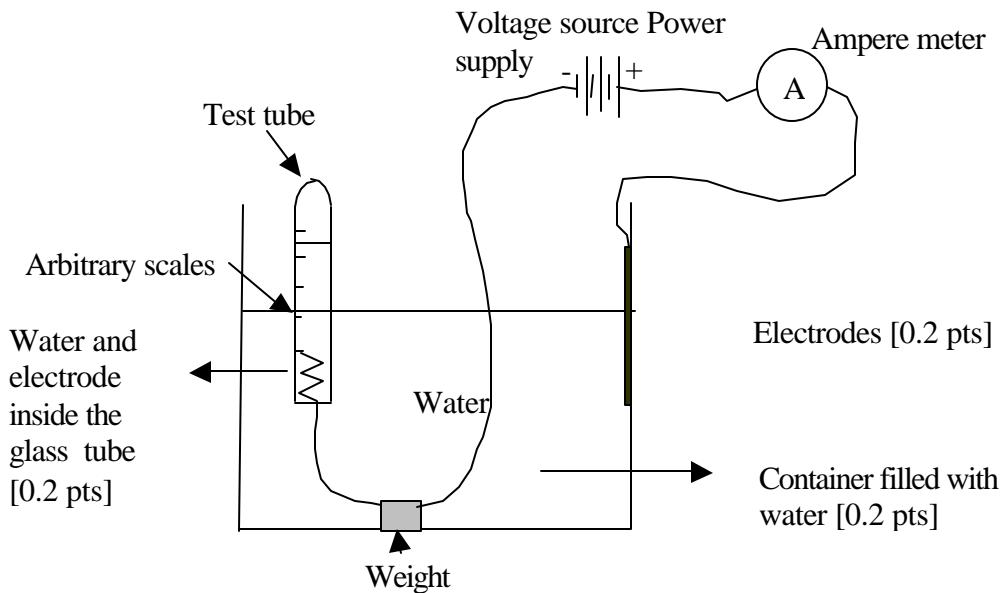
other legitimate methods may be used

## PART B

- ### 1. The experimental set up:[Total 1.0 pts]

[0.2 pts]

[0.2 pts]



2. Derivation of equation relating the quantities time  $t$ , current  $I$ , and water level difference  $Dh$ : **[Total 1.5 pts]**

$$I = \frac{\Delta Q}{\Delta t}$$

From the reaction:  $2 \text{H}^+ + 2 \text{e}^- \longrightarrow \text{H}_2$ , the number of molecules produced in the process ( $\Delta N$ ) requires the transfer of electric charge is  $\Delta Q = 2e \Delta N$  : [0.2 pts]

$$I = \frac{\Delta N}{\Delta t} 2e$$

[0.5 pts]

$$P \Delta V = \Delta N k_B T$$

[0.5 pts]

$$= \frac{I \Delta t}{2e} k_B T$$

$$P \Delta h(\mathbf{p}^*) = \frac{I}{2} \frac{\Delta t}{e} k_B T \quad [0.2 \text{ pts}]$$

$$I \Delta t = \frac{e}{k_B} \frac{2P(\mathbf{p}^2)}{T} \Delta h$$

[0.1 pts]

**3. The experimental data: [ Total 1.0 pts]**

| No. | $\Delta h$ (arbitrary scale) | I (mA) | $\Delta t$ (s) |
|-----|------------------------------|--------|----------------|
| 1   | 12                           | 4.00   | 1560.41        |
| 2   | 16                           | 4.00   | 2280.61        |
| 3   | 20                           | 4.00   | 2940.00        |
| 4   | 24                           | 4.00   | 3600.13        |

- The circumference  $\phi$ , of the test tube = 46 arbitrary scale [0.3 pts]
- The chosen values for  $\Delta h$  ( $\geq 4$  scale unit) for acceptable error due to uncertainty of the water level reading and for  $I$  ( $\leq 4$  mA) for acceptable disturbance [0.3 pts]
- # of data  $\geq 4$  [0.4 pts]

The surrounding condition ( $T, P$ ) in which the experimental data given above taken:

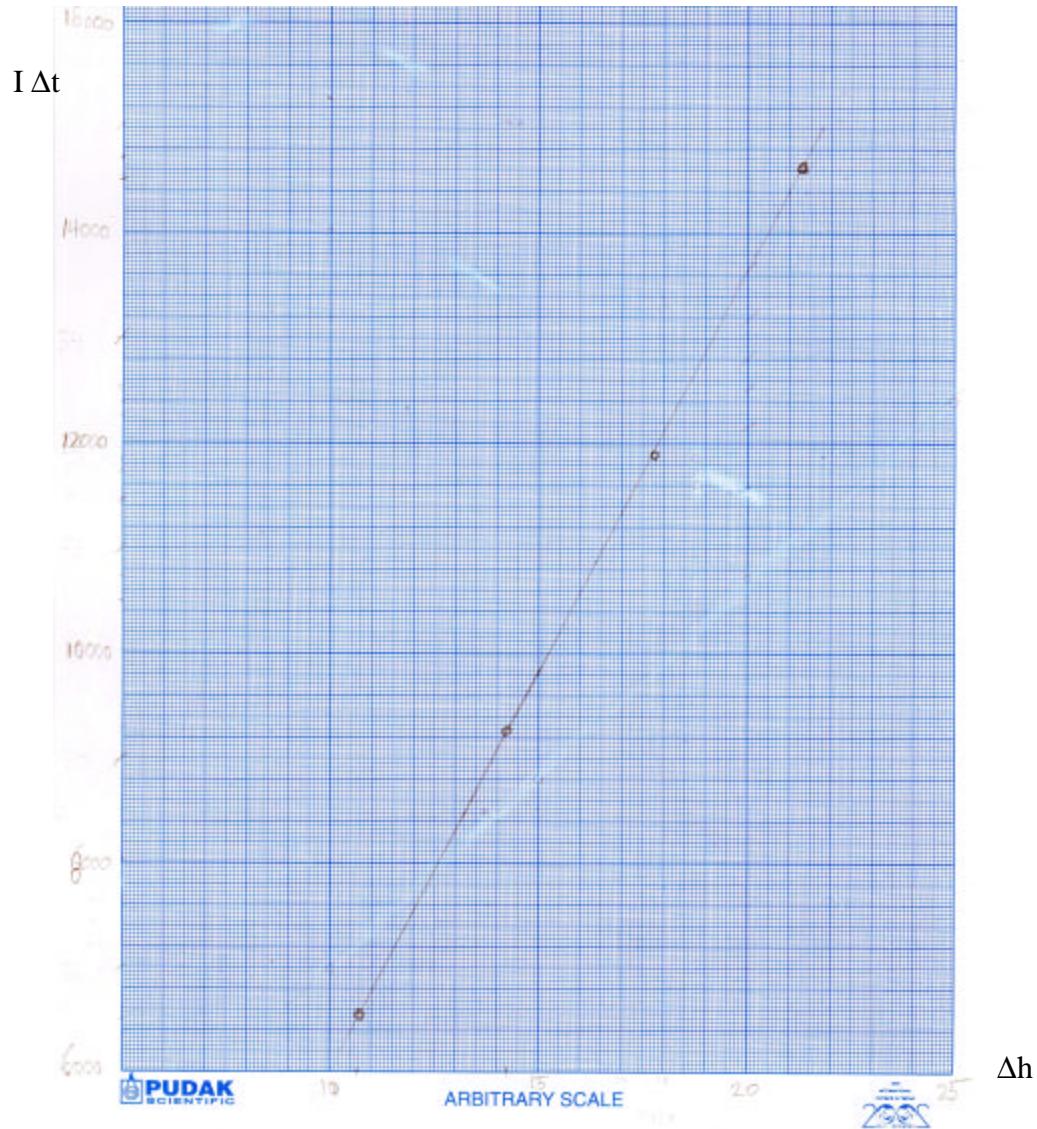
$$T = 300 \text{ K}$$

$$P = 1.00 \times 10^5 \text{ Pa}$$

**4. Determination the value of  $e/k_B$  [Total 1.5 pts]**

| No. | $\Delta h$ (arbitrary scale) | $\Delta h$ (mm) | I (mA) | $\Delta t$ (s) | $I \Delta t$ (C) |
|-----|------------------------------|-----------------|--------|----------------|------------------|
| 1   | 12                           | 10.68           | 4.00   | 1560.41        | 6241.64          |
| 2   | 16                           | 14.24           | 4.00   | 2280.61        | 9120.48          |
| 3   | 20                           | 17.80           | 4.00   | 2940.00        | 11760.00         |
| 4   | 24                           | 21.36           | 4.00   | 3600.13        | 14400.52         |

Plot of  $I\Delta t$  vs  $\Delta h$  from the data listed above



The slope obtained from the plot is 763.94;

$$\frac{e}{k_B} = \frac{763.94 \times 300 \times p}{2 \times 10^5 \times (23 \times 0.89 \times 10^{-3} \times 0.82)^2} = 1.28 \times 10^4 \text{ Coulomb K/J}$$

[1.0 pts]

Alternatively [the same credit points]

| No. | $\Delta h$ (mm) | $I\Delta t$ (C) | Slope    | $e/k_b$  |
|-----|-----------------|-----------------|----------|----------|
| 1   | 10.68           | 6241.64         | 584.4232 | 9774.74  |
| 2   | 14.24           | 9120.48         | 640.4831 | 10712.37 |
| 3   | 17.80           | 11760.00        | 660.6742 | 11050.07 |
| 4   | 21.36           | 14400.52        | 674.1816 | 11275.99 |

Average of  $e/k_b = 1.07 \times 10^4$  Coulomb K/J  
[1.0 pts]

| No. | $e/k_b$  | difference | Square difference |
|-----|----------|------------|-------------------|
| 1   | 9774.74  | -928.55    | 862205.5          |
| 2   | 10712.37 | 9.077117   | 82.39405          |
| 3   | 11050.07 | 346.7808   | 120256.9          |
| 4   | 11275.99 | 572.6996   | 327984.9          |

Estimated error [0.5 pts]

The standard deviation obtained is  $0.66 \times 10^3$  Coulomb K/J,  
Other legitimate measures of estimated error may be also used